MATH 122 Practice Exam 1

Instructions:

- 1. Print your name on this page in the space provided.
- 2. You must CIRCLE your final answer.
- 3. Show all work, write down the formulas used and explain in words what you are doing, partial credit will be given for written work only. Answers with no work will NOT be given full credit. Neatness counts.
- 4. Use of notes, books, OR calculators is not allowed.
- 5. Useful Identities:

$$\sin^{2}(x) = \frac{1}{2}(1 - \cos(2x))$$
$$\cos^{2}(x) = \frac{1}{2}(1 + \cos(2x))$$
$$\sin^{2}(x) + \cos^{2}(x) = 1$$
$$\tan(x) = \frac{\sin(x)}{\cos(x)}$$

6. Good luck!

Score	
1	/10
2	/10
3	/10
4	/10
5	/10
6	/10
7	/10
8	/0
Total	/70

Problem 1 (10 points)

Use partial fractions to evaluate:

$$\int \frac{1}{x^3 - 9x^2} \ dx$$

Problem 2 (10 points)

Evaluate the following integral using integration by parts.

$$\int y e^{3y} \ dy$$

Problem 3 (10 points)

Evaluate the following improper integral.

$$\int_0^\infty x e^{-x^2} \ dx$$

Problem 4 (10 points)

Evaluate the following integral using substitution.

$$\int y^7 (y^8 + 8)^{32} \, dy$$

Problem 5 (10 points)

Evaluate the following indefinite integral using the method of your choice. You must state what method you are using!

$$\int e^y \cos(y) \ dy$$

Problem 6 (10 points)

Evaluate the following definite integral using the method of your choice. You must state what method you are using!

$$\int_0^3 \frac{1}{(x-2)^2} \, dx$$

Problem 7 (10 points)

Evaluate the following integral using trigonometric substitution.

$$\int \frac{1}{\sqrt{1-4x^2}} \, dx$$

<u>Problem 8</u> (0 points) EXTRA CREDIT 5 POINTS

Starting from the product rule for differentiation, derive the formula for integration by parts. You must show all your work to get credit, no partial credit.