For each of the following equation:

- Find the Nullclines and plot them on Desmos to find fixed points. What are the possible cases for μ ?
- Solve exactly for the fixed points and confirm the cases that you found from the Nullclines.
- Find the Jacobian and discuss the stability of the fixed points in each of the different cases (if fixed points exist)
- Classify the type of bifurcation that you think is happening.
- Plot phase planes for each case including the bifurcation case. Can you explain what you see? Do you see ghost points and bottlenecks? Can you identify the manifolds?

$$\dot{x} = \mu x - x^2$$

$$\dot{y} = -y$$

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$$\dot{x} = \mu x - x^3$$

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$$\dot{x} = \mu x + x^3$$

$$\dot{y} = -y$$

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$$\dot{x} = y - 2x$$

$$\dot{y} = \mu + x^2 - y$$